

$$\sum_x Q(x) \log \frac{1}{P(x,y)} = \sum_x Q(x) \log \frac{1}{\frac{P(x,y)}{Q(x)}} + \sum_x Q(x) \log \frac{1}{Q(x)}$$

$$\frac{\text{energy}}{\text{temperature}} = \frac{\text{free energy}}{\text{temperature}} + \text{entropy}$$



*belief in
the system*



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rethinking entropy

$$\frac{1}{4} \log_2 4 + \frac{3}{4} \log_2 \frac{4}{3} \approx \frac{1}{4} \times 2 + \frac{3}{4} \times \frac{2}{5} \\ \approx \frac{10}{20} + \frac{6}{20}$$

knowledge gained

$$\log_2 \frac{1}{\frac{1}{8}} = \log_2 8 = \log_2 2^3 = 3$$

knowledge lens

$$\frac{1}{4} [\dots] + \frac{3}{4} [\dots]$$

$$- \sum_x Q(x) \log Q(x)$$

$$\log \frac{1}{Q(x)}$$

$$\sum_x Q(x) \dots$$

entropy is ambiguity

$$\frac{A}{B} = \frac{x \log_2 \frac{1}{x}}{(1-x) \log_2 \frac{1}{1-x}}$$

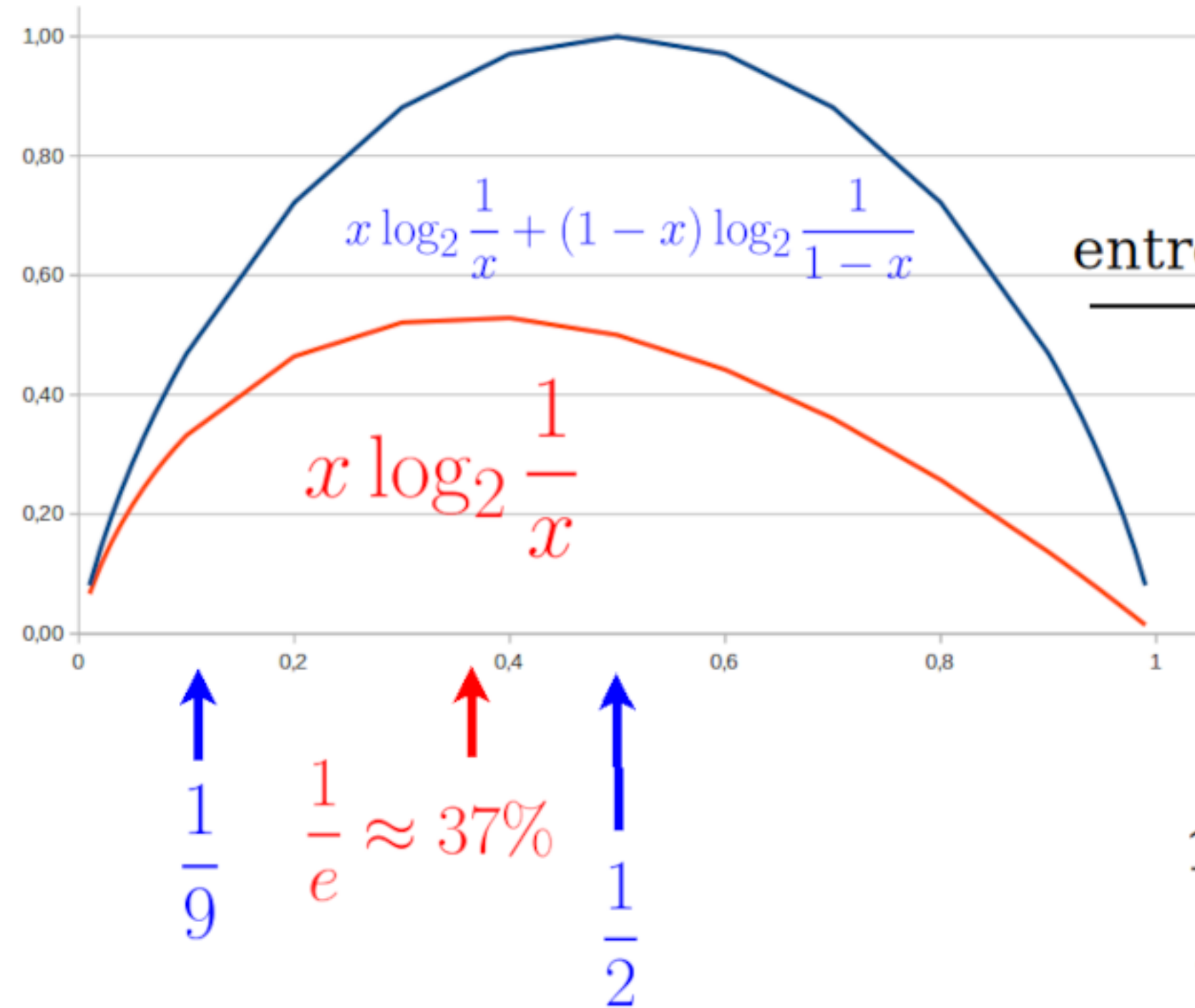
doubling

look at
 n equal probabilities $\frac{1}{n}$

$$\sum_{k=1}^n \frac{1}{n} \log_2 \frac{1}{\frac{1}{n}}$$

$$8 \left[\frac{1}{8} \log_2 \frac{1}{\frac{1}{8}} \right] = \log_2 8 = \log_2 2^3 = 3$$

$$64 \left[\frac{1}{64} \log_2 \frac{1}{\frac{1}{64}} \right] = \log_2 64 = \log_2 2^6 = 6$$



entropy	x	A/B
1	1/2	1
1/2	1/9	2.3
1/4	1/24	3.2
1/8	1/58	4.1
1/16	1/137	4.9
1/32	1/311	5.7
1/64	1/697	6.6
1/128	1/1540	7.3
1/256	1/3369	8.1

halving

look at 2 unequal probabilities x and $1-x$

energy

equilibrium

$$\ln p_i = \frac{-(E_i - \mathcal{E})}{k_B T} \quad \ln \frac{1}{p_i} = \frac{E_i - \mathcal{E}}{k_B T} \quad b = e^{\frac{1}{k_B T}}$$

interface

$$\sum_i p_i \log_b \frac{1}{p_i} = \sum_i p_i (E_i - \mathcal{E})$$

entropy expected energy

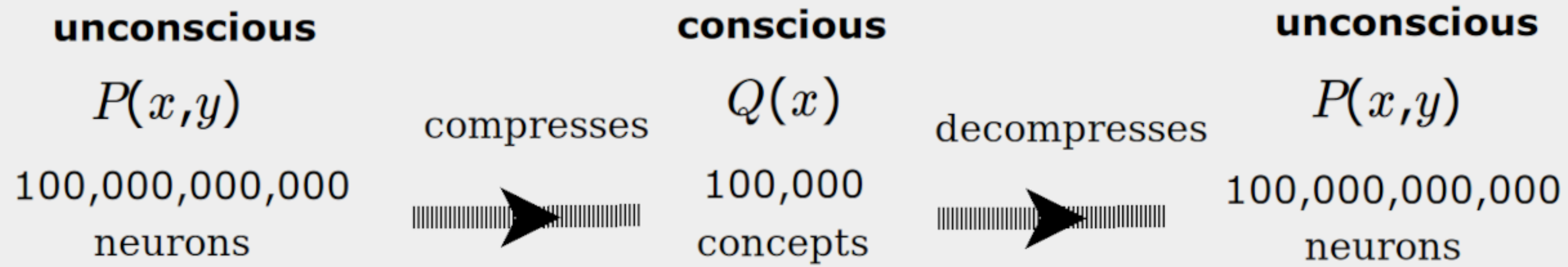
disequilibrium

$$\sum_i q_i \log_b \frac{1}{p_i} = \sum_i q_i (E_i - \mathcal{E})$$

expected energy

$$p_i = \frac{e^{\frac{-E_i}{k_B T}}}{\sum_i e^{\frac{-E_i}{k_B T}}} = e^{\frac{-(E_i - \mathcal{E})}{k_B T}}$$

Boltzmann distribution



$$\frac{1}{P(x,y)} = \frac{Q(x)}{P(x,y)} \frac{1}{Q(x)}$$

$$\log \frac{1}{P(x,y)} = \log \frac{1}{\frac{P(x,y)}{Q(x)}} + \log \frac{1}{Q(x)}$$

$$\sum_x Q(x) \log \frac{1}{P(x,y)} = \sum_x Q(x) \log \frac{1}{\frac{P(x,y)}{Q(x)}} + \sum_x Q(x) \log \frac{1}{Q(x)}$$

$$\frac{\text{energy}}{\text{temperature}} = \frac{\text{free energy}}{\text{temperature}} + \text{entropy}$$

$$\frac{Q(x)}{P(x,y)} = \frac{Q(x)}{P(x|y)} \frac{1}{P(y)}$$

$$\log \frac{1}{\frac{P(x,y)}{Q(x)}} = \log \frac{1}{\frac{P(x|y)}{Q(x)}} + \log \frac{1}{P(y)}$$

$$\sum_x Q(x) \log \frac{1}{\frac{P(x,y)}{Q(x)}} = \sum_x Q(x) \log \frac{1}{\frac{P(x|y)}{Q(x)}} + \sum_x Q(x) \log \frac{1}{P(y)}$$

$$\frac{\text{free energy}}{\text{temperature}} = \text{divergence} + \text{knowledge gained}$$



What is the optimal "cost of doing business"?


$$\frac{\text{electricity cost}}{\text{market cap}} = \frac{20 \text{ billion USD / year}}{2 \text{ trillion USD}} = 1\% \text{ every year}$$

belief in belief in the system
belief in the system

miners
entropy Quai
users
energy Qi

ALTERNATIVE

CUSTOMARY

y

evidence

evidence

x

inferred cause

inferred cause

$P(x,y)$

unconscious
backward-looking

generative model
predictive

$Q(x)$

conscious
forward-looking

approximation
optimized

gap between
unconscious and
conscious

boundary between
agent and
environment